

U.G. 6th Semester Examination-2022**PHYSICS****[HONOURS]****Discipline Specific Elective (DSE)****Course Code : PHY-H-DSE-T-03****(Digital Signal Processing)**

Full Marks : 40

Time : $2\frac{1}{2}$ Hours*The figures in the right-hand margin indicate marks.**Candidates are required to give their answers in their own words as far as practicable.***GROUP-A**

1. Answer any **five** questions : 2×5=10
- State the methods to find inverse z-transform.
 - Define ROC and explain its significance.
 - What is the meaning of radix-2?
 - What is FFT? Is it a transform?
 - Draw the signal flow graph for N = 4 radix-2 DIT-FFT algorithm.
 - Compare DIT and DIF-FFT algorithms.
 - Draw the signal flow graph for 4-point DIF-FFT algorithm.

- h) What are various methods to design IIR filters?

GROUP-B

2. Answer any **two** questions: 5×2=10

- a) Compute the DFT of the following sequence:

$$x(n) = \begin{cases} \frac{1}{4}, & 0 \leq n \leq 2 \\ 0, & \text{otherwise} \end{cases}$$

State Parseval's theorem. 3+2

- b) What are the advantages of z-transform? What is DFT? 3+2

- c) A discrete-time signal is expressed as $x(n) = \delta(n+1)2\delta(n) + 5\delta(n-3) - 2\delta(n-4)$.

Find its z-transform.

What is the difference between circular convolution and linear convolution? 3+2

- d) Find the inverse z-transform of $X(z) = \frac{3}{z-2}$ $|z| > 2$.

What are the applications of circular convolution? 3+2

GROUP-C

3. Answer any **two** questions: 10×2=20

- a) Compute the convolution $y(n)$ of the following signals:

$$x(n) = \begin{cases} \frac{1}{3}n & 0 \leq n \leq 6 \\ 0 & \text{otherwise} \end{cases} \quad \text{and} \quad h(n) = \begin{cases} 1, & -2 \leq n \leq 2 \\ 0, & \text{otherwise} \end{cases}$$

Examine whether the following signal:

$x(n) = \cos\left(\frac{n}{10}\right) \cos\left(\frac{n\pi}{10}\right)$ is a periodic signal or not. A digital filter has the following impulse response: $h(n) = \{-3, 2, 1, -2, 3\}$. If it is a linear phase filter, justify. 5+3+2

- b) Determine the circular convolution of the following sequences:

$$x(n) = \{1, 0.5, 1, 0.5, 1, 0.5\}$$

$$h(n) = \{0, 1, 2, 3\}$$

Sketch the following signal

$$x(t) = A \sin t \text{ for } -\infty < t < \infty.$$

Also check whether the signal is a power signal or an energy signal or neither. What are Energy and Power Signals? Explain. 5+3+2

- c) Explain the different properties of region of convergence (ROC) of z-transform. Test the system $y(n) = x(n).u(n)$ for Linearity, Causality and Time invariance. Define region of convergence (ROC). 5+4+1

- d) State the advantages and disadvantages of digital filters. Use the rectangular window to design a linear FIR filter of order $N = 24$ to approximate the following frequency response magnitude.

$$|H_d(e^{j\omega})| = \begin{cases} 1 & \text{for } |\omega| \leq 0.2\pi \\ 0 & \text{for } 0.2\pi \leq |\omega| \leq \pi \end{cases}$$

What is DIF-FFT algorithm? 5+4+1
