554/Math. UG/4th Sem/MATH-H-SEC-T-2A&B/22

## U.G. 4th Semester Examination - 2022

# **MATHEMATICS**

## [HONOURS]

**Skill Enhancement Course (SEC)** 

**Course Code: MATH-H-SEC-T-2A&B** 

Full Marks: 40 Time: 2 Hours

The figures in the right-hand margin indicate marks.

The symbols and notations have their usual meanings.

Answer all the questions from selected Option.

### **OPTION-A**

## MATH-H-SEC-T-2A

- 1. Answer any **five** questions:  $2 \times 5 = 10$ 
  - a) In a graph, define pendent vertex and degree of a vertex.
  - b) Find the number of edges in  $K_{m,n}$ . Define component of a graph.
  - c) Find the number of circuits in  $K_n$   $(n \ge 3)$ .
  - d) If a graph has exactly two odd vertices, then which of the following is true?

- i) There is an Euler's circuit.
- ii) There is an Euler path.

Justify your answer.

- e) Draw the adjacency and incidence matrix of a square. Define weighted graph.
- f) Define regular graph with *n* vertices. Find the relation of regular graph with complete graph.
- g) If a graph has x vertices and y edges, then find the number of branches and chords with proper argument.
- h) Define vertex deleted and edge deleted subgraph of a graph.
- 2. Answer any **two** questions:  $5 \times 2 = 10$ 
  - Prove that in a graph if there is exactly two odd vertices then there must be a path joining them.
  - b) Let G(n,m) be a graph on vertices  $v_i, i = 1, 2, ..., n$ . Let  $G v_i$  has  $e_i$  edges for i = 1, 2, ..., n. Show that
    - $i) \qquad m = \frac{\sum\limits_{i=1}^{n} e_i}{n-2}$
    - ii)  $\deg(v_i) = \{\sum_{i=1}^n \frac{e_i}{n-2}\} e_i, i = 1, 2, \dots, n.$

- c) Prove that a tree having *n* vertices contains *n*–1 edges.
- 3. Answer any **two** questions:  $10 \times 2 = 20$ 
  - a) What do you mean by simple graph? Prove that a simple graph *G* has a spanning tree if and only if *G* is connected. Define Hamiltonian cycle. How it differs from normal cycle?

b) State Dijkstra's algorithm to find the shortest path. What do you mean by isomorphic graph? Draw all non-isomorphic trees of 6 vertices. Explain travelling salesman method.

Prove that a connected graph with n vertices and e edges contains a unique cycle if and only if n = e. Prove that the number of odd vertices in a graph is always even. 3+3+2+2

### **OPTION-B**

#### MATH-H-SEC-T-2B

## (Linux)

1. Answer any **five** questions:

 $2 \times 5 = 10$ 

- a) Name two commercial distros of Linux operating system.
- b) What is the difference between a command and a system call?
- c) What is deadlock?
- d) What is the use of *man* command in Linux?
- e) Which Linux command can be used to show the status of a process? Give example.
- f) What is the use of wild card characters? Give an example.
- g) What is *umask*?
- h) What is the use of *sudo* command?
- 2. Answer any **two** questions:

 $5\times2=10$ 

- a) Write a short note on Linux user management.
- b) Discuss the INODE file system structure in Linux.
- c) Explain the use of environment variables with suitable examples.

3. Answer any **two** questions:

- $10 \times 2 = 20$
- a) Explain different memory management commands in Linux with example.
- b) Write the commands used for the following purposes with examples:
  - i) Displaying content of a text file
  - ii) Modifying access permissions of files
  - iii) Displaying disk space usage
  - iv) Deleting a directory
  - v) Searching some pattern from a file.
- c) Explain the roles of the following system calls in Linux with examples:
  - i) exec ii) sleep iii) fstat iv) brk v) alarm

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